for k=1,…,K-1